
Ballistic Motion Planning

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Overview

- Motivation
- ***Paper 1: Ballistic Motion Planning***
- ***Paper 2: Single Leg Dynamic Motion Planning with Mixed-Integer Convex Optimization***
- Summary
- Quiz

Motivation

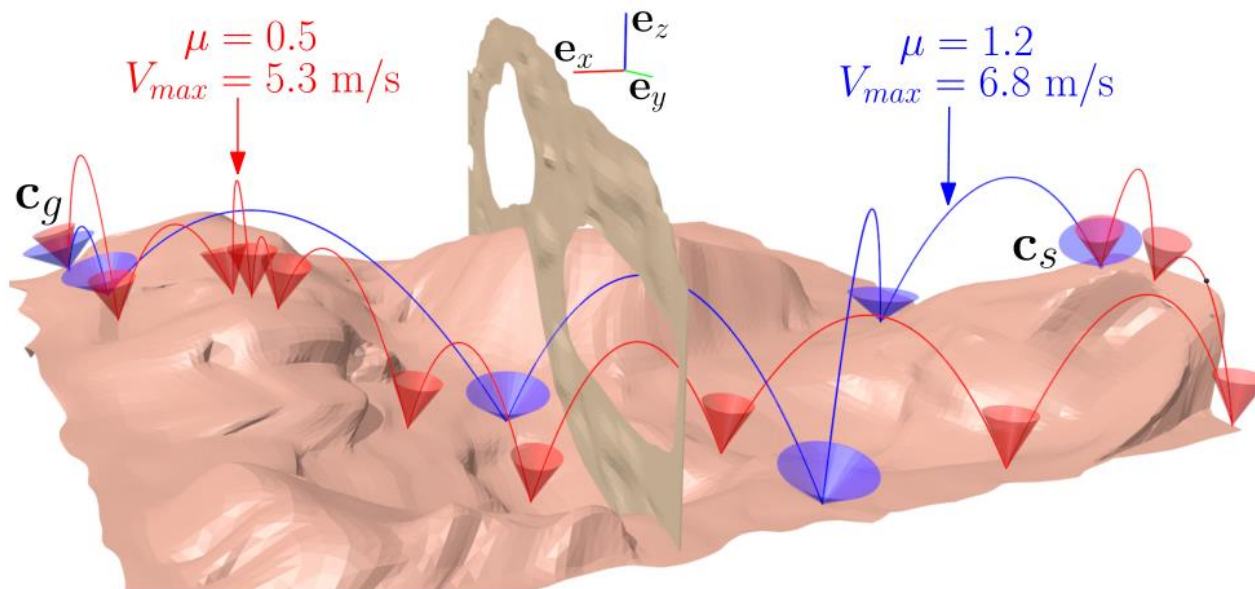
- Jumping motion introduces new shortcuts
 - Instead of going around an obstacle block, why not jump over it?
- Unreachable locations can become reachable
- This would increase complexity for the path planning algorithm

Paper 1: **Ballistic Motion Planning**

Mylene Campana | Jean-Paul Laumond
IROS 2016

Key Features

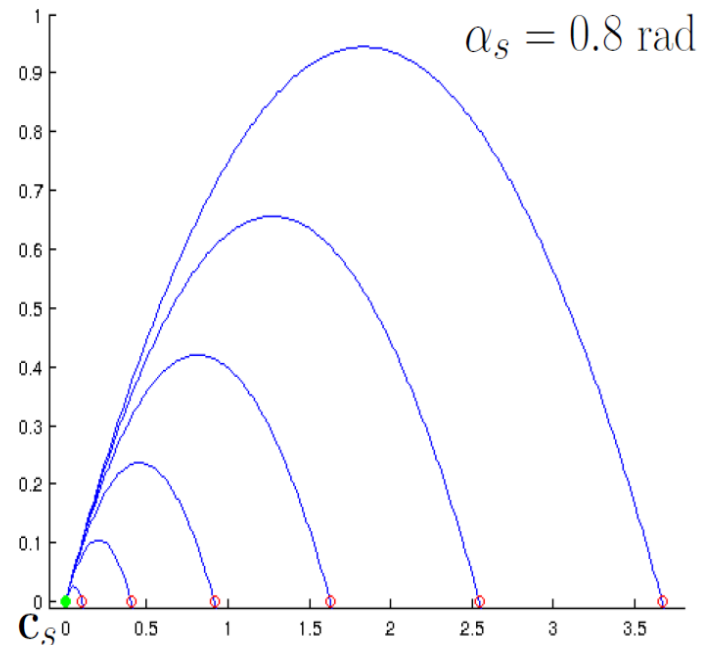
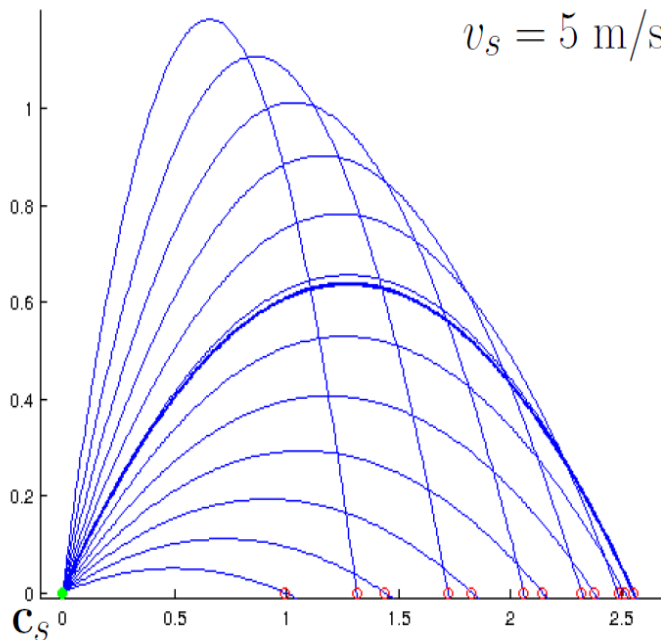
- Developed a motion planning algorithm for **jumping point robot** in arbitrary environment considering **slipping and velocity** constraints



Accessible Space

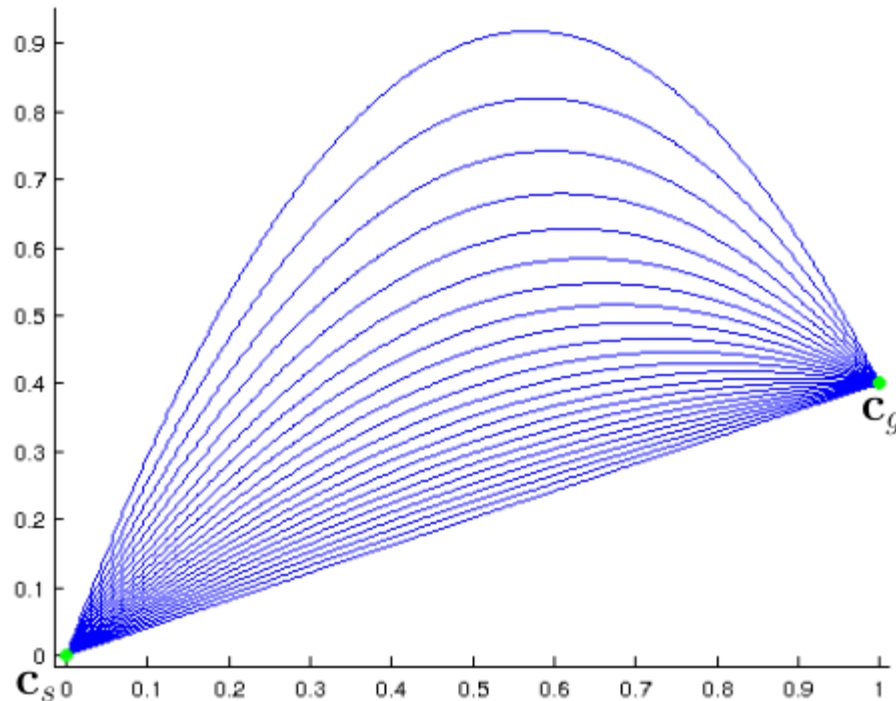
- Parabola trajectory is determined by **takeoff angle** and **initial velocity**

$$\mathbf{c}(t) = -\frac{g}{2} t^2 \mathbf{e}_z + \dot{\mathbf{c}}_s t + \mathbf{c}_s$$



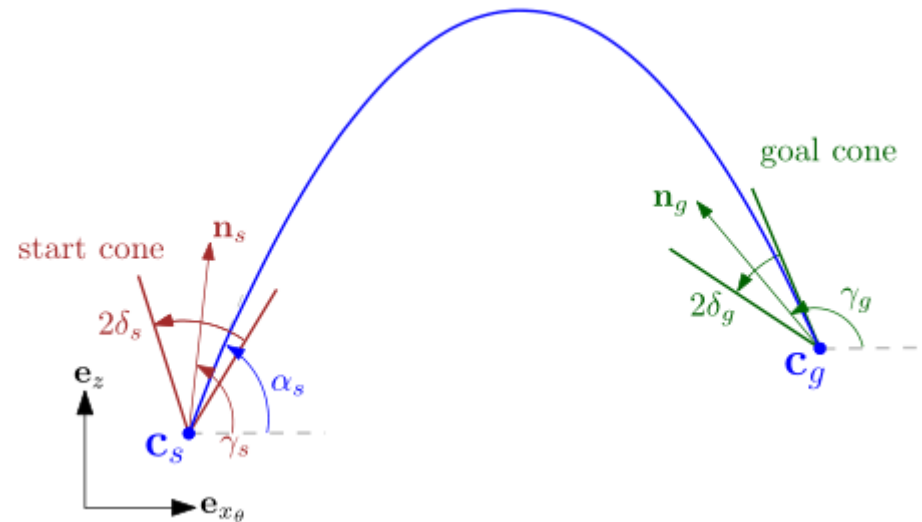
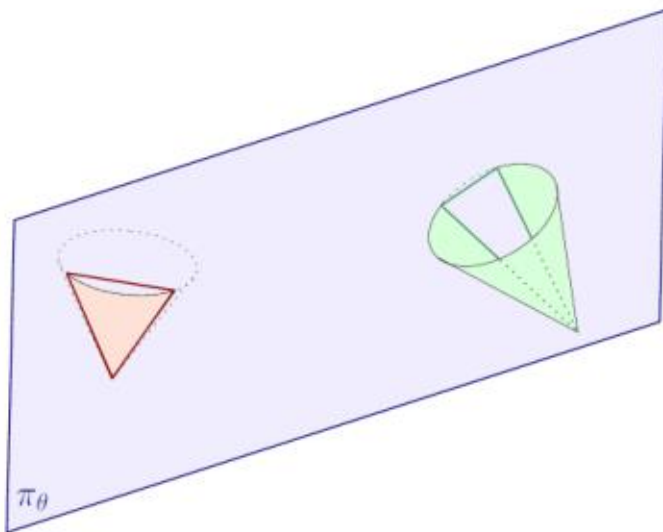
Goal Oriented Ballistic Motion

- **Physically-feasible parabolas** linking c_s and c_g with varying takeoff angles



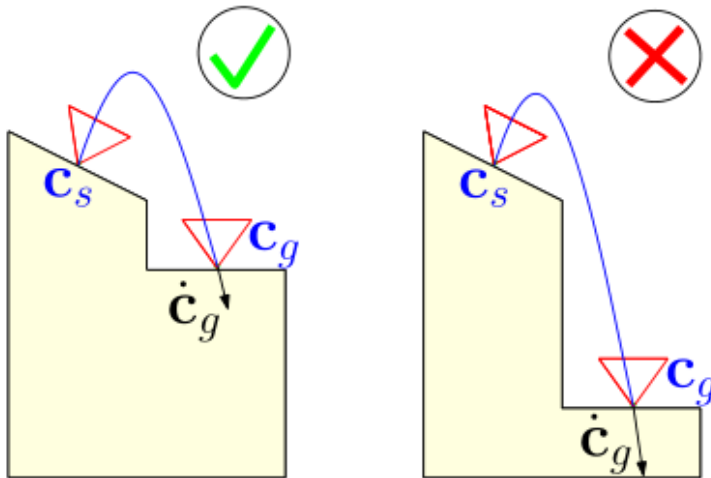
Non-sliding Constraints

- Intersection between parabola plane and friction cones

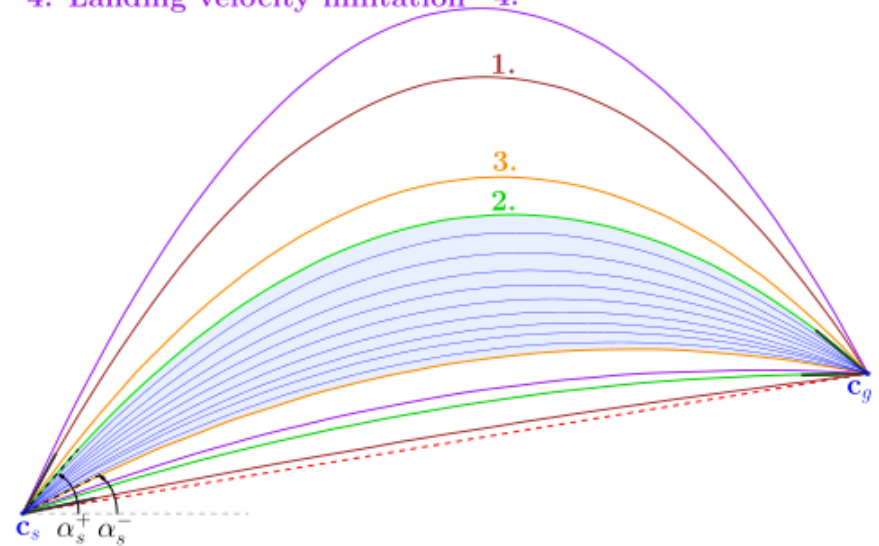


Velocity Constraints

- $v_s \leq V_{max}$
- $\begin{cases} \alpha_3^- = (V_{max}^2 - \sqrt{\Delta})/gX_\theta \\ \alpha_3^+ = (V_{max}^2 + \sqrt{\Delta})/gX_\theta \end{cases}$



1. Takeoff from initial cone
2. Landing in final cone
3. Takeoff velocity limitation
4. Landing velocity limitation



Motion Planning

- Probabilistic Roadmap Planner
 - Build Roadmap
 - Link nodes with Steer algorithm
 - Over when start and goal position are connected
- Steer Algorithm
 - Selection of takeoff angle
- Beam Algorithm
 - Computes all possible parabola paths
 - Outputs range of permissible angles

Results

- https://www.youtube.com/watch?v=vw_K7HqANmk&feature=youtu.be

Strengths and Limitations

- Small computational cost
- Arbitrary environment

- Point robot representation limitation
 - No stance dynamics
- Frictionless Jumps

Paper 2: Single Leg Dynamic Motion Planning with Mixed-Integer Convex Optimization

Yanran Ding | Chuanzheng Li | Hae-Won Park
IROS 2018

Key Features

- Used **mixed-integer convex programming** formulation for dynamic motion planning
- Capable of planning consecutive jumps through challenging terrains



Phases of Jumping Robot

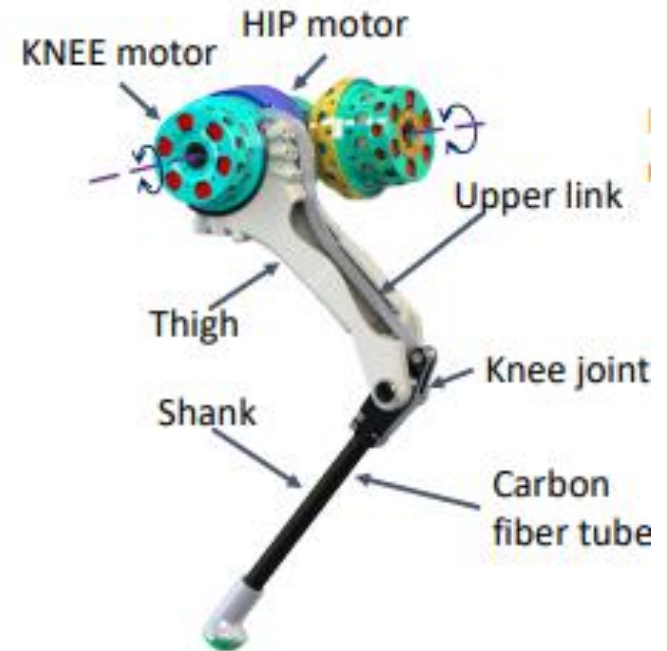
- Stance Phase
 - Leg is in contact with the ground
 - Actuators to apply force
- Flight Phase
 - Follows ballistic motion
 - Choosing foot holds

Constraints

- Joint Torques do not exceed actuator limits
- Goal region should be reached at the end of the motion
- Ground reaction force (GRF) must be within friction cone

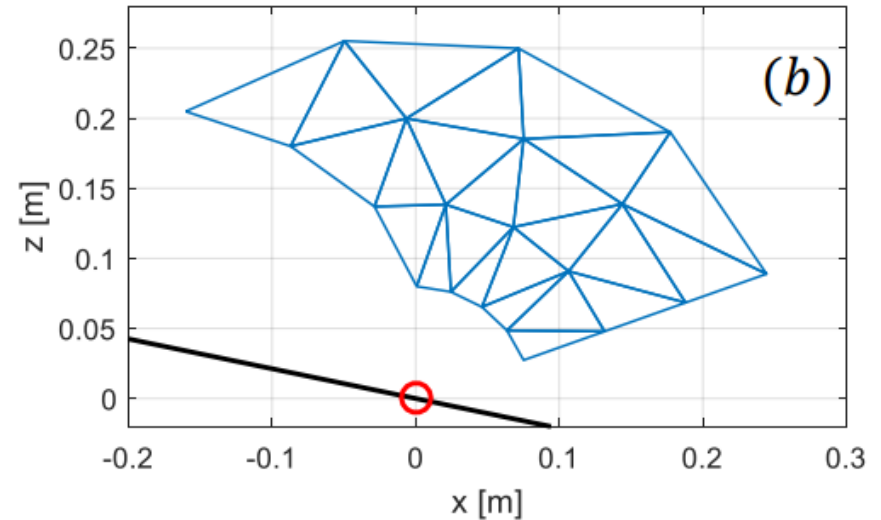
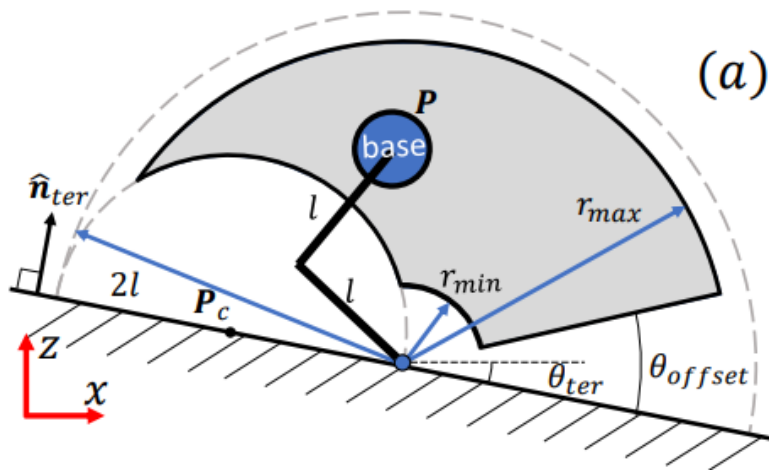
Point Mass Dynamic Model

- To simplify dynamics
- Center of Mass assumed to be in the Base Center



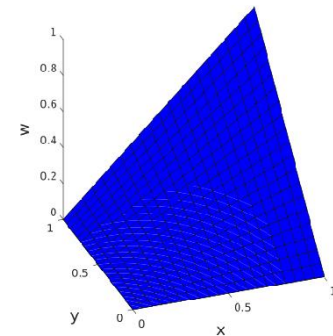
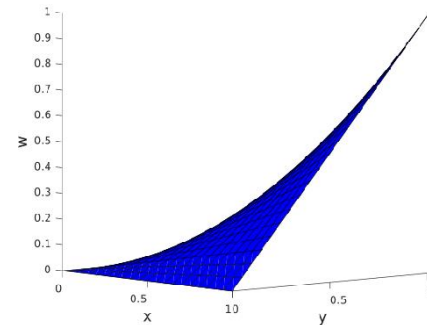
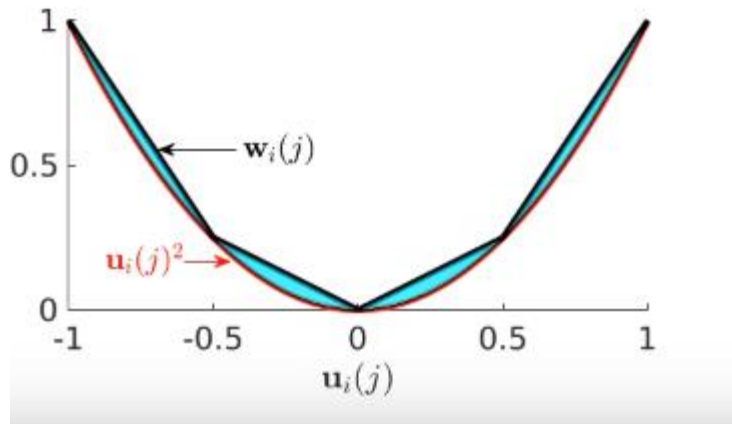
Mixed-integer Convex Torque Constraint

- Workspace Discretization



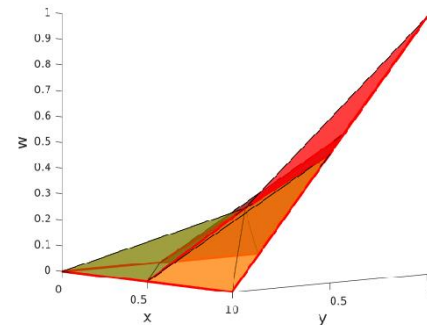
Background: Mixed Integer Convex Optimization

- Non-convex optimization to convex optimization

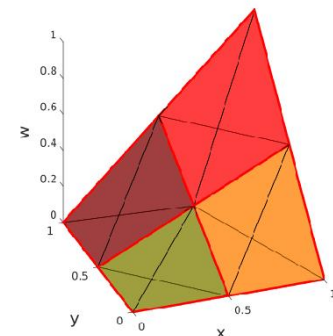


(a)

(b)



(c)

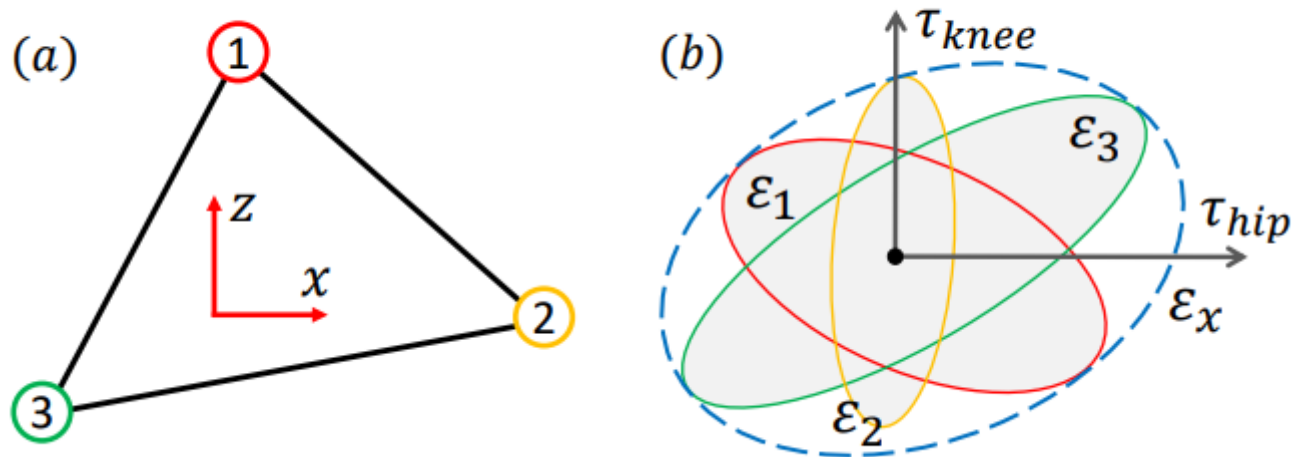


(d)

Mixed-integer Convex Torque Constraint

- Convex Outer-Approximation of Torque Ellipsoid

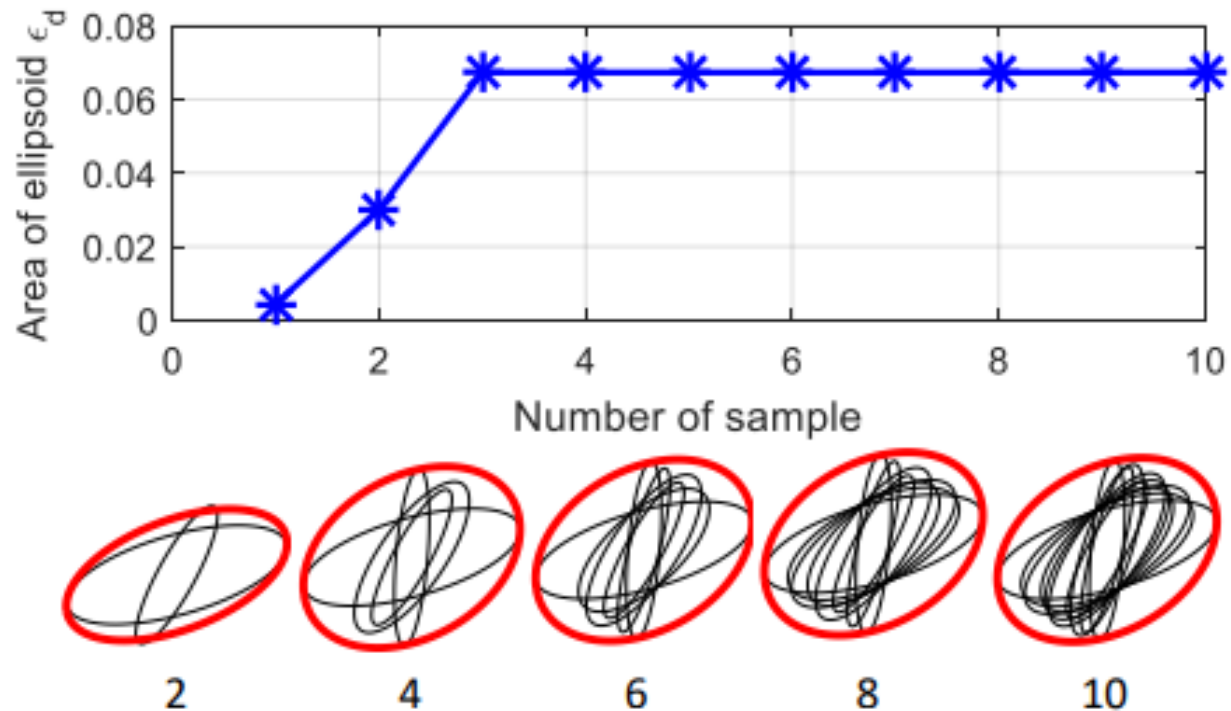
$$\|J^T(\mathbf{p}) \cdot \mathbf{F}\|_\infty \leq \tau_{max}$$



$$\mathbf{F}^T \mathbf{J}_n \cdot \mathbf{J}_n^T \mathbf{F} \leq \mathbf{F}^T \mathbf{X} \mathbf{F}, \quad \forall n$$
$$\mathbf{F}^T \mathbf{X} \mathbf{F} \leq \tau_{max}^2$$

Mixed-integer Convex Torque Constraint

- Convex Outer-Approximation of Torque Ellipsoid

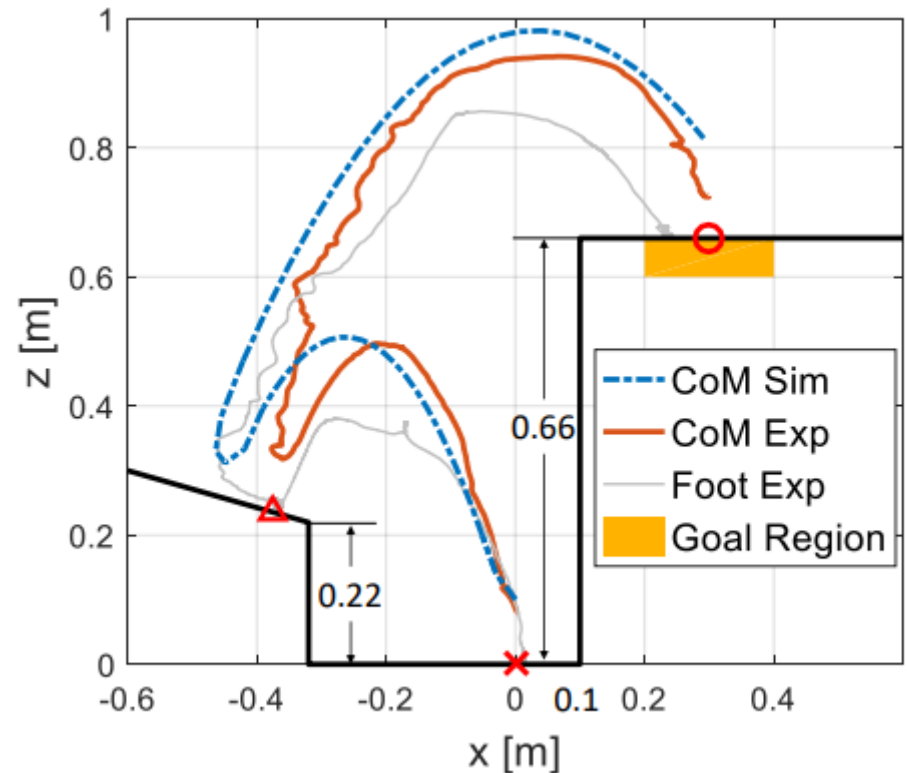
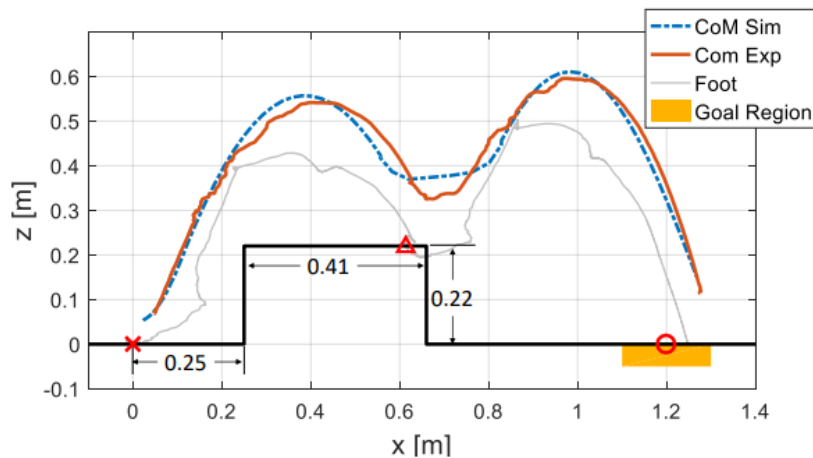


Other Implementation

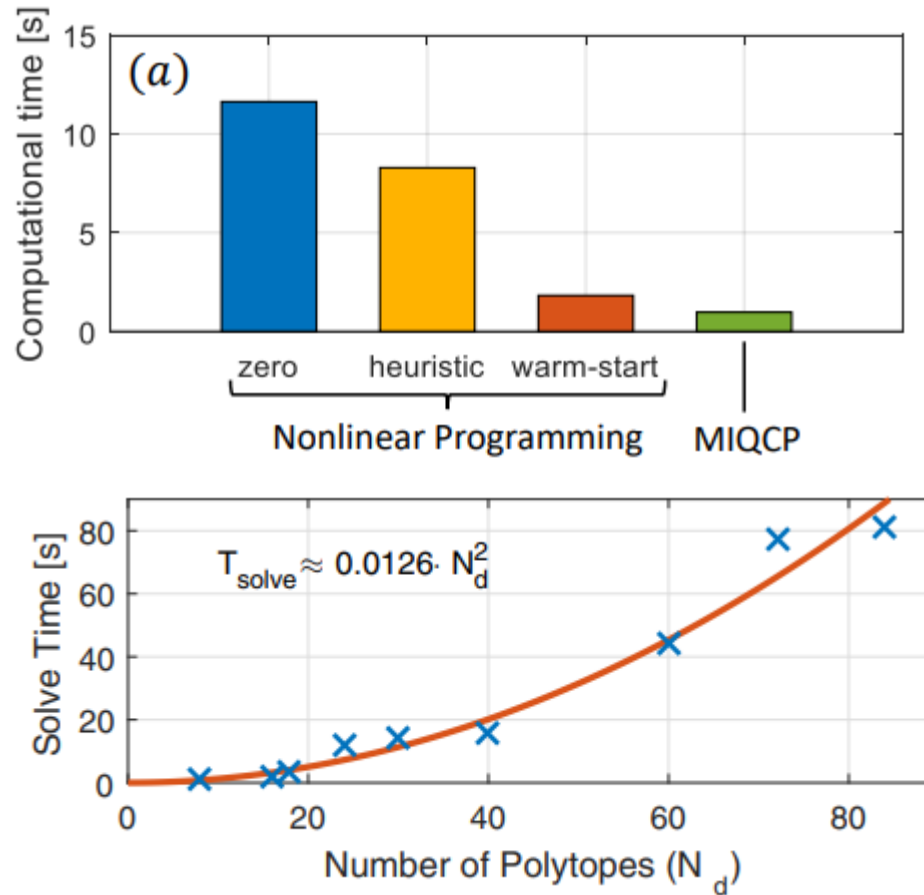
- McCormick Envelope Approximation
- Foothold Position choice
- GRF Constraints

Results

- <https://www.youtube.com/watch?v=0pFYjoUKGu0>



Performance



Summary

Summary

- Paper 1: Ballistic Motion Planning
 - Jumping point robot navigating in 3d environment
 - 2 constraints due to the friction cone
 - Constraint to limit takeoff velocity -> robot's speed capacity
 - Constraint to limit landing velocity -> impact force tolerance
- Paper 2: Single Leg Dynamic Motion Planning with Mixed-Integer Convex Optimization
 - Implemented ballistic motion planning for a real robot and simplifies the non-convexity of actuator torque constraint through Mixed-Integer Convex Optimization